

A combination mode of the annual cycle and the El Niño/Southern Oscillation

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The El Niño/Southern Oscillation (ENSO) is characterized by two main states: El Niño events defined by positive sea surface temperature anomalies in the eastern tropical Pacific Ocean and La Niña events marked by cooler surface temperatures in the same region. ENSO is broadly considered to be an oscillatory instability of the coupled ocean-atmosphere system in the tropical Pacific 1-6 that shows a tight interaction with the seasonal cycle, El Niño events typically peak in the boreal winter, but the mechanism governing this phase synchronization⁷ is unclear. Here we show, using observational data and climate model experiments, that the nonlinear atmospheric response to combined seasonal and inter-annual sea surface temperature changes gives rise to a near-annual combination climate mode with periods of 10 and 15 months. Specifically, we find that the associated southward shift of westerly wind anomalies during boreal winter and spring triggers the termination8 of large El Niño events. We conclude that combination mode dynamics and related shifts in western tropical Pacific rainfall patterns occur most prominently during strong El Niño events.

Present ENSO theories, such as the recharge oscillator paradigm⁹, although very successful in explaining some observational features of ENSO, do not account for the interaction between interannual and seasonal timescales. In particular, they do not provide any insight into why strong El Niño events peak towards the end of the calendar year (in December–January–February: DJF) and terminate in the subsequent months. Previous extensions to these theories that rely on nonlinear concepts^{10–13}, such as subharmonic frequency locking and frequency entrainment, nonlinear resonance, the quasi-periodic transition to chaos or parametric excitation^{7,14,15}, capture some aspects of ENSO/annual cycle interactions.

None of these extended dynamical systems' concepts, however, describes the observational finding¹⁶ that a weakening and southward shift of westerly wind anomalies on the Equator accompanies the termination of strong El Niño events. Numerous modelling studies^{8,17–20} have confirmed this observational evidence, thus supporting the notion of strong annual cycle/ENSO interactions originating in the tropical western Pacific. Here, we set out to provide a simple unifying dynamical framework to understand various aspects of ENSO, such as the physics of seasonally paced El Niño transitions, spectral characteristics and ENSO's hydroclimatic impacts.

The seasonal weakening and southward shift of westerly wind anomalies that contributes to the transition between El Niño

and La Niña can be readily described in terms of an empirical orthogonal function (EOF) decomposition of the tropical wind anomaly field^{8,21} for the observational period 1958–2001. The first EOF (EOF1) is the equatorially quasi-symmetric 10 m wind pattern associated with ENSO (Fig. 1a), featuring the anomalous Walker circulation, as characterized by equatorial westerly wind anomalies in the western Pacific (positive phase of the first principal component PC1, Fig. 1e) during El Niño. PC1 is well correlated (r = 0.86) with the commonly used Niño 3.4 index (sea surface temperature (SST) anomalies averaged over $120^{\circ} \, \text{W}-170^{\circ} \, \text{W}$ and $5^{\circ} \, \text{S}-5^{\circ} \, \text{N}$).

The second EOF (Fig. 1b), in combination with the positive phase of PC2 (termination phase of strong El Niño events, Fig. 1f), captures the development of the anomalous Philippine anticyclone²², along with a strong meridional shear of anomalous zonal wind across the Equator and a southward-shifted westerly wind anomaly⁸. It plays an important role in terminating El Niño events⁸ by re-establishing the upwelling regime in the equatorial eastern Pacific (the abrupt weakening of equatorial westerly wind anomalies triggers an upwelling Kelvin wave) and by discharging heat away from the Equator into the Northern Hemisphere owing to the off-equatorial wind stress curl pattern^{8,23}. This is highlighted by the tight connection between PC1 and PC2 during the peak phase of strong El Niño events (Fig. 1e, fand Supplementary Fig. S3).

To further elucidate this connection between PC1 and PC2, the power spectra of the observed PCs are calculated (Fig. 2a and Supplementary Figs S1a and S2). The PC1 spectrum shows pronounced levels of variability mostly in the interannual period band of 2–8 years, in contrast to PC2, which exhibits a significant spectral peak at a period of \sim 15 months and a weaker one at \sim 10 months. Transforming the frequency axis of the PC1 spectrum (hereafter represented by f) to 1-f and 1+f, where 1 represents the annual frequency, we find that the peak of PC2 aligns well with the shifted $1-f_{\rm E}$ peak of PC1, where $f_{\rm E}$ denotes the frequency band of ENSO ($f_{\rm E}=1/2\,{\rm yr}^{-1}$ to $1/8\,{\rm yr}^{-1}$). A multi-century-long simulation with an ENSO-resolving coupled climate model captures the EOF2 pattern, PC2 time evolution, its phase relationship with PC1 and key spectral characteristics (Supplementary Figs S6–S10).

Spectral peaks at frequencies $1-f_{\rm E}$ and/or $1+f_{\rm E}$ on either side of the annual frequency are characteristics of near-annual combination tones (the difference and sum tone, respectively) that originate from an amplitude modulation of the annual cycle due to ENSO; or in mathematical terms from the product between ENSO and the annual cycle, or more complicated variants thereof. Combination tones were first described in acoustic theory during the eighteenth

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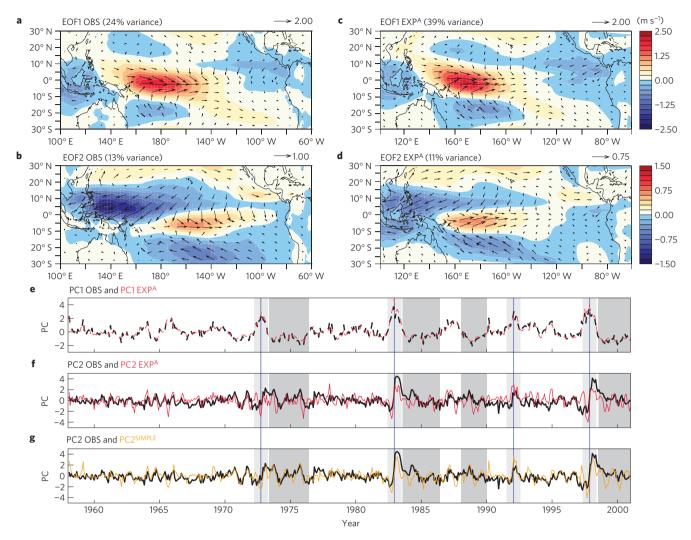


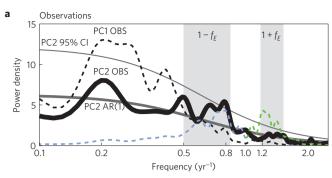
Figure 1 | **Tropical Pacific surface wind modes. a-d**, Dominant pattern of wind variability (zonal wind as shading) in the tropical Pacific obtained by an EOF decomposition of observed (**a,b**) and simulated (**c,d**) 10 m wind anomalies. **e,f**, Normalized principal components (PCs) for observations (OBS) and experiment (EXP_A). Blue rectangles indicate the duration (0.5 σ threshold of PC1 OBS) of the four strongest El Niño events (determined by maximum PC1 OBS amplitude). Blue vertical lines highlight the event peak times. Grey rectangles indicate the duration (-0.5 σ threshold of PC1 OBS) of the four strongest La Niña events (determined by minimum PC1 OBS amplitude). **g**, The same as in **e**, **f** but for PC2 OBS (black) and PC2_{SIMPLF} (orange).

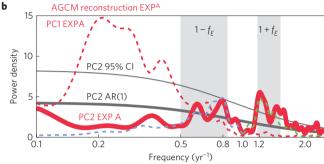
and nineteenth century^{24,25}. Later, they were invoked to understand aspects of glacial cycles²⁶ and ENSO¹³. Near-annual spectral power has been identified in oceanic and atmospheric observations^{22,27}. However, the exact physical origin and climatic relevance of these near-annual spectral peaks and the corresponding physical mode have so far gone unnoticed in studies of tropical climate.

On the basis of these spectral characteristics of wind PC2 we propose that the mechanism responsible for seasonally paced El Niño terminations is provided by a new combination mode (C-mode) of tropical Pacific climate. It emerges from the nonlinear interaction between seasonal cycle and interannual ENSO variability, primarily through an atmospheric nonlinearity, such as the nonlinear dissipation of momentum in the planetary boundary layer associated with the seasonal development of the South Pacific Convergence Zone⁸ (SPCZ) or the advection of low-level moisture.

To test this hypothesis we conduct a 10-member ensemble of sensitivity experiments with an atmospheric general circulation model (AGCM), forced with only an SST seasonal cycle and time-evolving ENSO-related SST anomalies (EXP_A), associated with wind PC1. In addition, we conduct a single-member experiment with the same ENSO SST forcing but without a seasonal cycle in SST (perpetual autumn equinox experiment PERP).

The AGCM-simulated ensemble mean wind EOF1 (Fig. 1c) reveals a very close similarity to the observed EOF1 (Fig. 1a) and high correlation between the corresponding PCs (r = 0.95). The pronounced correspondence between simulated and observed EOF2 wind pattern (Fig. 1b,d) and the corresponding principal components during major El Niño events (Fig. 1f) confirms EOF2 as a C-mode resulting from the nonlinear interaction (product) between ENSO and the annual cycle. Moreover, the fact that the spatial structure of EOF2 is largely reproduced by this experiment further documents that the initiation of the Philippine anticyclone and the southward shift of the anomalous equatorial westerlies in DJF and their evolution in subsequent months are both manifestations of the nonlinear combination mode. The evolution of the simulated PC2 (Fig. 1f and Supplementary Fig. S3) documents a rapid transition at the end of the calendar year from negative to positive values during strong El Niño events, very similar to the observed PC2. The perpetual equinox experiment does not exhibit the characteristic atmospheric circulation response related to the combination mode (Supplementary Figs S3 and S4), thus demonstrating that the annual cycle of SST is a key element of the atmospheric combination mode response. Our results confirm and extend earlier modelling studies 17,18 that found that a fixed





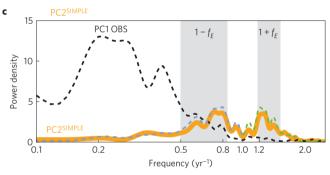


Figure 2 | Power spectra for PC1 and PC2 using the Blackman-Tukey method. Frequency is abbreviated to f. To illustrate the PC2 combination tone frequencies, PC1 was shifted to 1-f (dashed blue) and 1+f (dashed green) and scaled by a factor 1/3. Grey rectangles indicate the near-annual combination tone frequency bands $1-f_{\rm E}$ and $1+f_{\rm E}$. The AR(1) null hypothesis for the PC2s in $\bf a$ and $\bf b$ is shown by a thick grey line and the 95% confidence interval (CI) indicated by a thin grey line. $\bf a$, Observed PC1 and PC2. $\bf b$, Averaged experiment EXP_A PC1 and PC2. $\bf c$, Observed PC1 and PC2_{SIMPLE}.

ENSO SST anomaly pattern together with an SST seasonal cycle was sufficient to simulate a southward shift of the ENSO-related wind anomalies in boreal winter and spring.

The power spectrum of the simulated ensemble PC2 average from EXP_A (Fig. 2b and Supplementary Fig. S1b) reveals combination tone frequency peaks at $1-f_{\rm E}$ (\sim 15 months) and $1+f_{\rm E}$ (\sim 10 months). As expected for a combination mode between ENSO and the annual cycle, we find a spectral gap for annual frequencies. In addition, we integrated the AGCM for 150 years with the annual cycle and ENSO-related SST anomalies (EXPB) obtained from EOF1 of a 500-year-long coupled pre-industrial control simulation (PICTRL). The results (Supplementary Figs S6-S10) show two very well pronounced spectral peaks for PC2 of the winds at combination tone frequencies. The two peaks match those from the fully coupled simulation (PC2 from PICTRL) and those from the shifted PC1 spectra of EXP_B (Supplementary Fig. S9). The AGCM experiments (EXP_A and EXP_B), the fully coupled model run PICTRL and the observations all exhibit very similar EOF2 wind structures (Fig. 1b,d and Supplementary Fig. S6b,d); however, there are slight differences in the prominence of spectral power in the $1-f_{\rm E}$ and $1+f_{\rm E}$ bands. These differences may be related to different representations of atmospheric nonlinearities and the reddening effect of air–sea coupling, which may act to favour a stronger $1-f_{\rm E}$ peak over $1+f_{\rm E}$. The power spectrum of the perpetual autumn equinox AGCM experiment exhibits neither the characteristic $1-f_{\rm E}$ nor the $1+f_{\rm E}$ combination tone frequency peaks in the PC2 spectra (Supplementary Fig. S5), thus supporting the evidence that the annual cycle in SST is a key component for the second EOF mode.

To further verify our combination mode hypothesis, we consider a theoretical approximation to the C-mode in the form of $PC1_{OBS}(t) \times \cos(\omega_a t - \varphi)$, which comes from the lowest-order term of the atmospheric nonlinearity. Here ω_a denotes the angular frequency of the annual cycle and φ represents a one-month phase shift. This time series, labelled as $PC2_{SIMPLE}$, by its mathematical nature, exhibits pronounced $1-f_E$ and $1+f_E$ spectral peaks (Fig. 2c and Supplementary Fig. S1c). Furthermore, it shows remarkable agreement with the observed PC2, especially during El Niño events (Fig. 1g and Supplementary Fig. S3). The correlation coefficient between $PC2_{SIMPLE}$ and the observed PC2 is 0.51 and between $PC2_{SIMPLE}$ and the averaged PC2 from experiment EXP_A, is 0.67. The observed PC2 can thus be viewed as $PC2_{SIMPLE}$ (Fig. 2c) superimposed on atmospheric white noise (Fig. 2b and Supplementary Fig. S11) and further reddened by air—sea coupling (Fig. 2a).

The seasonal development of the SPCZ in DJF has previously been shown to be a key element in generating the observed southward wind anomaly shift⁸ during strong nonlinear El Niño events. During the 1982/1983, 1991/1992 and 1997/1998 El Niño events the SPCZ collapsed into a zonal equatorial rain band with strongly increased precipitation on the Equator and anomalous drying in the tropical northwest Pacific (Fig. 3a). These zonal SPCZ events^{28,29} cause severe precipitation impacts in South Pacific island nations and influence Asian monsoon systems by changing the spatial distribution of diabatic heating. We find that C-mode dynamics are responsible for the spatial precipitation pattern during these events (Fig. 3c,d).

In the present study we demonstrate that a series of climatic features occurring during the peak and termination phase of large El Niño events can be explained by a previously overlooked near-annual combination mode resulting from the nonlinear interaction between seasonal and interannual SST forcing. These features include the Philippine anticyclone²² (Fig. 1b), zonal SPCZ events²⁸ (Fig. 3) and the southward shift of the westerly wind anomalies at the end of calendar year¹⁶, which strongly contributes to the termination of large El Niño events⁸.

Notably, the combination mode dynamics, as represented by PC2 of wind anomalies (Fig. 1e), occurs prominently for strong El Niño events and is less pronounced for weak El Niño events and La Niña events²¹. This amplitude asymmetry may explain why La Niña conditions are not characterized by a strong phase synchronization with the seasonal cycle and why they can last for much longer than strong El Niño events discussed above (Fig. 1e). Once an El Niño event reaches a certain amplitude, its demise after DJF becomes highly predictable (Fig. 1g) and largely controlled by the C-mode. This is in contrast with the predictability of El Niño's onset phase, which is characterized by the stochastic occurrence of westerly wind bursts and other short-term phenomena³⁰. Thus, studying the C-mode may help improve the ENSO performance in climate models and increase the skill of seasonal climate predictions.

Methods

Precipitation analysis. Using the Global Precipitation Climatology Project (GPCP V2.2) precipitation product for the period 1979–2000³¹, we reconstruct the anomalous austral summer precipitation fields for the three strongest wind PC2 anomaly events (1982/1983, 1991/1992, 1997/1998) by multiplying the respective rainfall regression pattern with the DJF-mean values of the corresponding PCs (Fig. 3). Adding the anomalous rainfall associated just with PC1 during these events

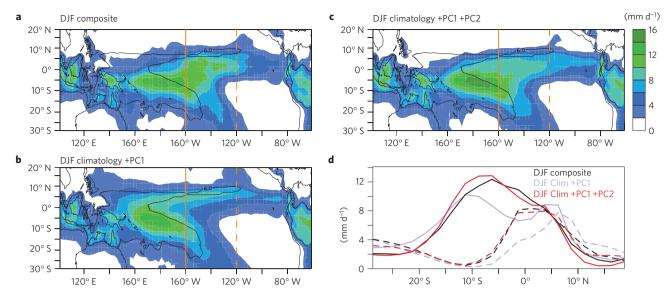


Figure 3 | **El Niño precipitation changes.** The climatological DJF-mean 6 mm d⁻¹ precipitation contour for the period 1979-2000 indicates the SPCZ extent during DJF (**a-c**). **a**, Precipitation composite average for the three strongest PC2 anomaly events: 1982/1983, 1991/1992 and 1997/1998. **b**, Climatological precipitation plus the precipitation composite associated with the observed PC1 for these events. **c**, Climatological precipitation plus the precipitation composite associated with both observed PC1 and PC2 for these events. **d**, Precipitation across 160° W (solid) and 120° W (dashed) for **a-c**: DJF composite (black), DJF climatology plus PC1 precipitation (blue-grey) and DJF climatology plus PC1 and PC2 precipitation (red).

to the DJF-mean climatological rainfall results in an intensification of precipitation in some regions (Fig. 3b), but not the strong equatorial enhancement seen during zonal SPCZ events (Fig. 3a). Adding both the rainfall anomalies associated with the wind PC1 and PC2 (Fig. 3c) to the DJF-mean climatology results in the characteristic zonal orientation and eastward extension of zonal SPCZ events, very similar to the composite (Fig. 3a), as well as the northwestern Pacific drying. This illustrates that the wind PC2 is an excellent indicator of zonal SPCZ events.

Combination tones. The two main nonlinear atmospheric processes in the tropical region are the dissipation of momentum in the planetary boundary layer and low-level moisture advection. These processes serve as exemplary sources of the atmospheric nonlinearity that can produce the combination tones. The anomalies in these two nonlinear processes give rise to anomalous momentum and moisture source terms containing $\mathbf{v_A} \cdot \mathbf{v_E}$ and $\mathbf{v_A} \cdot \nabla q_E + \mathbf{v_E} \cdot \nabla q_A$, respectively. Here \mathbf{v} denotes horizontal velocity and ∇q the moisture gradient field. The subscripts A and E denote the fields associated with the annual cycle and ENSO respectively. If one considers simple sinusoid time evolutions for these two source terms, these will be proportional to $A_A \cos(\omega_A t) A_E \cos(\omega_E t)$, where A_E and ω_E denote ENSO amplitude and angular frequency, respectively, and A_A and ω_A amplitude and angular frequency of the annual cycle. Thus, these types of quadratic nonlinear process allow ENSO to interact with the annual cycle to produce the sum and difference (combination) tones:

$$A_{\rm A}\cos(\omega_{\rm A}t)A_{\rm E}\cos(\omega_{\rm E}t) = \frac{1}{2}A_{\rm A}A_{\rm E}\{\cos([\omega_{\rm A}-\omega_{\rm E}]t)+\cos([\omega_{\rm A}+\omega_{\rm E}]t)\}$$

This mechanism operates in a similar way if we consider a frequency range for ENSO instead of a simple sinusoid. $PC2_{SIMPLE}$ is the mathematical representation of the quadratic combination mode between ENSO (PC1) and the annual cycle. As such it serves as our base hypothesis. We show that PC2 EXP_A (Fig. 2b) is essentially $PC2_{SIMPLE}$ plus atmospheric white noise with a small red component (Supplementary Fig. S11). For consistency, we test both the observed and experiment PC2s against a red-noise null hypothesis (Fig. 2a,b and Supplementary Fig. S1a,b). Another test of PC2 EXP_A against white noise can be found in Supplementary Fig. S11.

Full Methods (detailing the model experiments and spectral analysis) are available in the Supplementary Information.

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Author contributions

M.F.S., F-F.J. and A.T. designed the study. M.F.S. conducted the experiments, performed the analysis and wrote the initial draft of the manuscript. All authors discussed the results and helped improve the manuscript.

Additional information

Supplementary information is available in the online version of the paper. Reprints and permissions information is available online at www.nature.com/reprints. Correspondence and requests for materials should be addressed to M.F.S. or F-F.J.

Competing financial interests

The authors declare no competing financial interests.