# Greenhouse

Global Warming Science, EPS101

**Camille Hankel and Eli Tziperman** 

https://courses.seas.harvard.edu/climate/eli/Courses/EPS101/

## Class objectives

- How natural greenhouse gases keep the Earth from freezing
- How human-added greenhouse gasses lead to warming
- How can such small changes in  $CO_2$  concentration (currently 420 ppmv  $\approx$  0.04% by volume) make such a big difference
- How greenhouse gases work on the molecular level
- The water vapor feedback
- The logarithmic dependence of warming on CO<sub>2</sub>
- How important are other greenhouse gasses relative to CO<sub>2</sub>

#### Global Warming Science 101, Greenhouse, Camille Hankel & Eli Tziperman Radiative forcing (RF)

RF is the net increase in the energy input to the climate system due to greenhouse gas increase, in watts/m<sup>2</sup>.

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**Figure 8.6** (a) Radiative forcing (RF) from the major well-mixed greenhouse gases (WMGHGs) and groups of halocarbons, 1850-2011, (b) as (a) but with a log scale.

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a) All Anthropogenic Gases co. Radiative Forcing (W m<sup>-2</sup>) 1.0 0.5 CH₄  $N_2O$ Others 0.0 1850 1900 1950 2000 b)Main Gases Radiative Forcing (W m<sup>-2</sup>) CO. 10<sup>-1</sup> CH₄  $N_2O$ HCFC Halocarbon 10<sup>-2</sup> HFC CFC 10<sup>-3</sup> 1850 1900 2000 1950

**Figure 8.6** (a) Radiative forcing (RF) from the major well-mixed greenhouse gases (WMGHGs) and groups of halocarbons, 1850-2011, (b) as (a) but with a log scale.

#### (IPCC AR5, 2013)

RF is the net increase in the energy input to the climate system due to greenhouse gas increase, in watts/m<sup>2</sup>. **Observed radiative forcing increases** 

**More specifically:** (IPCC AR5, 2013) RF: the change in net downward radiative flux at the tropopause after allowing for stratospheric temperatures to readjust to radiative equilibrium, while holding surface and tropospheric temperatures, and water vapor and cloud cover, fixed at the unperturbed values.





(IPCC AR5, 2013)

Global Warming Science 101, Greenhouse, Camille Hankel & Eli Tziperman Future scenarios for radiative forcing:

The Representative Concentration Pathway (RCP)



**Figure 8.22** | Global mean anthropogenic forcing. (solid lines with circles are net; long dashes with squares are ozone; short dashes with diamonds are aerosol; dash-dot are WMGHG; colors: RCPs with **red for RCP8.5, orange RCP6.0, light blue RCP4.5, and dark blue RCP2.6**). Symbols: times of ACCMIP simulations were performed.

### Workshop #1: Observed and projected increase in greenhouse gasses

## Observations & projections of CO<sub>2</sub> concentration



#### Figure 2.1: CO<sub>2</sub> time series.

Annually averaged CO<sub>2</sub> concentration, observed and projected according to different RCP scenarios.

## Observed vs projected CO<sub>2</sub> concentrations



**Figure 8.5** (above) Time evolution of global-averaged mixing ratio of long-lived species 1850–2100 following each RCP; blue (RCP2.6), light blue (RCP4.5), orange (RCP6.0) and red (RCP8.5). (Meinshausen et al., 2011b)

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## Observed vs projected CO<sub>2</sub> concentrations

worse than RCP8.5 business as usual considered in 2011



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### Energy balance: Albedo, greenhouse



FIGURE 9.4. Earth's energy balance (from Trenberth, K.E., and D.P. Stepaniak, 2004: The flow of energy through the Earth's climate system. **Q.J.R.Meteorol.Soc.**, **130**, 2677-2701).

### Notes sections 2.1.1, 2.1.2, 2.1.3: Energy balance, 2-layer model, continuous temperature profile and level of last absorption

(use next three slides)

## Energy balance of the Earth Step 1: no atmosphere!!



# Energy balance of the Earth







Outgoing

LW= $\sigma T_s^4$ 

long wave

Incoming

shortwave

Reflected

shortwave

SW=LW

# Energy balance of the Earth

Step 1: no atmo





## The Greenhouse Effect Step 2: add a 1-layer atmosphere



• Two unknowns: surface temperature T and (mid) atmospheric temperature  $T_a$ . Two equations (energy balance at the surface and at mid-atmosphere):

$$\frac{S_0}{4}(1-\alpha) + \epsilon \sigma T_a^4 = \sigma T^4$$

$$\epsilon \sigma T^4 = 2\epsilon \sigma T_a^4.$$

$$T = \left(\frac{(S_0/4)(1-\alpha)}{\sigma(1-\epsilon/2)}\right)^{1/4} = T_0(1-\epsilon/2)^{-1/4} = 284 \text{ K} = 13 \text{ °C}$$

 Result: surface temperature increases due to the "greenhouse effect"



Surface

#### Workshop #2 a,b: 2-layer energy balance model

# The Anthropogenic Greenhouse Io1, Greenhouse, Camille Hankel & Eli Tziperman

Step 3: add a continuous atmospheric temperature profile



- Level of last absorption: where most of the radiation emitted upward escapes to space, without getting absorbed again
- Increasing greenhouse gas ➡ Rising level of last absorption ➡ Earth radiates from a colder temperature ➡ Energy balance is broken: LW < SW ➡ The temperature must adjust</li>

## The Anthropogenic Greenhouse, Camille Hankel & Eli Tziperman Chore Or Color Or Color

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# The Anthropogenic Greenhouse Camille Hankel & Eli Tziperman

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#### Workshop #2 c: emission height: leave for HW

How greenhouse gasses work: wavelength-dependent radiation & molecular energy levels

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## Black body radiation

Planck's law of black-body radiation:  $B(\lambda, T) = \frac{2hc^2}{\lambda^5} \frac{1}{e^{\frac{hc}{\lambda k_B T}} - 1}$ 

 $B(\lambda,T)d\lambda$  is the energy per area/ time/ angle emitted between wavelengths  $\lambda \& \lambda + d\lambda$ ; T=temperature; h=Planck's const; c=speed of light; k=Boltzmann's const.

Total emitted radiation per area/ time:  $\sigma T^4$  Stefan–Boltzmann constant:  $\sigma = 5.670367 \times 10^{-8} \text{ W} \cdot \text{m}^{-2} \cdot \text{K}^{-4}$ 



https://en.wikipedia.org/wiki/File:Wiens\_law.svg

#### Global Warming Science 101, Greenhouse, Camille Hankel & Eli Tziperman Shortwave vs longwave radiation

Earth's surface and the sun both emit blackbody radiation according to Planck's function — they radiate over the full spectrum



#### **Figure 2.5: Blackbody radiation.**

(a) Planck's black-body spectral radiance for the emission temperatures of the Earth (blue) and Sun (red), as a function of wavelength. (b) blue curve shows estimated outgoing longwave radiation at the top of the atmosphere as a function of wavenumber, with black-body radiation curves at different temperatures shown by dashed lines. The deviations from the 287 K black body radiation curve indicate absorption bands due to  $CO_2$ ,  $CH_4$ ,  $H_2O$ , and  $O_3$ ; the central  $CO_2$  absorption line is shown on both panels as a vertical gray bar.

## How do greenhouse gases work?



https://youtu.be/sTvqlijqvTg

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## Vibration energy levels of $CO_2 \& H_2O$





**CO**<sub>2</sub>

 $H_2O$ 

http://davidobru.blogspot.com/2017/01/some-animations.html

http://www.dynamicscience.com.au/tester/solutions1/ chemistry/greenhouse/co2andtheghe.htm

The vibration energy levels determine the frequency of absorption

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The vibration energy levels determine the frequency of absorption

# Greenhouse gasses vibration modes

- Discrete wavelengths excite molecular transitions in greenhouse gas molecules
- This results in absorption and re-emission of radiation of that wavelength
- The "transition wavelengths" for various greenhouse gases have been measured in lab experiments







Symmetric Stretch 1366 cm<sup>-1</sup>

Bending Mode 667 cm<sup>-1</sup>

Asymmetric Stretch 2349 cm<sup>-1</sup>



http://butane.chem.uiuc.edu/pshapley/GenChem1/L15/2.html

#### Global Warming Science 101, Greenhouse, Camille Hankel & Eli Tziperman Molecular vibration/rotation energy levels & photon absorption



Photon energy:  $E = h\nu = hc/\lambda$  where *h* is Planck's constant, *c* is the speed of light,  $\nu$ the frequency, and  $\lambda$  the wavelength. Note:  $\nu = c/\lambda = 1/T$ , where T is the wave period.

From "ocean optics" web book,

https://www.oceanopticsbook.info/view/absorption/physics-of-absorption

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# Absorption cross-section

- Spike in absorption "efficiency" i.e. cross-section at wavenumber that excites a molecular transition: spikes called <u>absorption lines</u>
- Absorption "lines" look like Gaussian/Lorentzian  $(\alpha_L/\pi)/((\nu \nu_0)^2 + \alpha_L^2)$  profiles due to "line broadening"
  - Pressure broadening due to molecular collisions
  - Doppler broadening due to gaussian distribution of particle velocities
- All individual lines calculated and broadened in radiative transfer code to give "absorption spectrum" for a greenhouse gas



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#### Notes section 2.2.3: Broadening

(use next three slides)

#### Global Warming Science 101, Greenhouse, Camille Hankel & Eli Tziperman Pressure/Collisional Broadening



#### Global Warming Science 101, Greenhouse, Camille Hankel & Eli Tziperman Pressure/Collisional Broadening



















#### Doppler Broadening (significantly weaker in Earth's atmosphere)





https://forum.huawei.com/enterprise/en/what-isthe-doppler-effect/thread/510221-100305

CO<sub>2</sub> molecule moves toward photon  $\Rightarrow$  photon seems at higher frequency  $\Rightarrow$  molecule absorbs a photon of lower frequency than that of absorption line. CO<sub>2</sub> molecule moves away from photon  $\Rightarrow$  opposite

The random motion of the gas molecules causes the widening of absorption lines because molecules that happen to be moving towards/away from the incoming photon will see it at a different frequency/ wavelengths.



note absorption windows...

Workshop #3 radiative forcing

#### Notes sections 2.2.4, 2.2.5: logarithmic dependence, global warming potential

(use next 5 slides)

#### Logarithmic dependence of RF on CO<sub>2</sub>

The absorption is typically proportional to the radiation intensity at any given location, and therefore the equation for the transmitted radiation, I(x), may be written as  $dI/dx = -\mu I$ , where  $\mu$  depends on the absorbing medium. The solution for the radiation intensity along the pipe is, therefore,

$$I(x) = I_0 e^{-\mu x} \quad I_0 \longrightarrow I(x) \qquad \qquad \bigcirc$$

For CO<sub>2</sub>, the RF varies logarithmically with concentration. We showed in section 3.2 that the warming and radiative forcing are approximately linearly related. This implies that the temperature response also depends logarithmically on the CO<sub>2</sub> concentration. We, therefore, write, schematically,

$$T = T_0 + A \log_2(\mathrm{CO}_2/280)$$

which implies:

$$T_{\times 2} - T_{\times 1} = A \log_2(2CO_2/280) - A \log_2(CO_2/280) = A \log_2 2 = A,$$

$$T_{\times 4} - T_{\times 2} = A \log_2(4 \text{CO}_2/280) - A \log_2(2 \text{CO}_2/280) = A \log_2 2 = A.$$

That is, each doubling of CO<sub>2</sub> leads to the same increase in temperature!

#### What about other greenhouse gases?

How do we quantify their effect relative to that of CO<sub>2</sub>?

# IR absorption of the major greenhouse, Camille Hankel & Eli Tziperman



https://en.wikipedia.org/wiki/Absorption\_band

CO<sub>2</sub> & water vapor absorbs the most IR, at different wavelengths

GWP: the time-integrated RF due to a pulse emission of a GHG, relative to a pulse emission of an equal mass of  $CO_2$ 

IPCC, Climate Change 2013, Chapter 8

GWP: the time-integrated RF due to a pulse emission of a GHG, relative to a pulse emission of an equal mass of CO<sub>2</sub>

The GWP of a greenhouse gas is its radiative forcing effect relative to  $CO_2$ , given its lifetime and strength as an absorber over a specified time horizon (TH).

IPCC, Climate Change 2013, Chapter 8

G

GWP: the time-integrated RF due to a pulse emission of a GHG, relative to a pulse emission of an equal mass of  $CO_2 \ r TH$ 

WP(x) = 
$$\frac{\int_{0}^{TH} a_x \cdot [x(t)] dt}{\int_{0}^{TH} a_r \cdot [r(t)] dt}$$

The GWP of a greenhouse gas is its radiative forcing effect relative to  $CO_2$ , given its lifetime and strength as an absorber over a specified time horizon (TH).

x(t): time-dependent decay of a GHG; r(t): that of CO<sub>2</sub>;  $a_{x,r}$ : RF per 1 kg (W/m<sup>2</sup>/kg).

IPCC, Climate Change 2013, Chapter 8

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an absorber over a specified time horizon (TH).

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$$GWP(x) = \frac{J_0}{c'}$$

$$\frac{\int_0^{TH} a_x \cdot [x(t)] dt}{\int_0^{TH} a_r \cdot [r(t)] dt}.$$

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 $\langle 1 \rangle$ 

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$$\Delta T(t) = \sum_{i} \int_{0}^{t} E_{i}(s) A$$

IPCC, Climate Change 2013, Chapter 8

#### Global Warming Science 101, Greenhouse, Camille Hankel & Eli Tziperman Other GHG: Global Warming Potential (GWP)

GWP: the time-integrated RF due to a pulse emission of a GHG, relative to a pulse emission of an equal mass of CO<sub>2</sub> r TH

GWP of a greenhouse gas is its forcing eff CO2, considering its lifetime and its strength as an absorber, over a specified time horizon (TH).

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wikipedia

dt

GWP values and ifetimes	Lifetime in years	<b>Global Warming Potential (GWP)</b>		
		20 years	100 years	500 years
lethane	12.4	86	34	
litrous oxide (N <sub>2</sub> O)	121.0	268	298	
litrous oxide (N <sub>2</sub> O)	121.0	264	265	
IFC-134a hydrofluorocarbon)	13.4	3790	1550	

# Notes sections 2.2.6: water vapor feedback

(use next 2 slides)

#### The water vapor feedback

First, a reminder: the Clausius-Clapeyron relation



The saturation water vapor increases exponentially with temperature, at about 6%/ °C



Direct radiative forcing of absorption by water vapor molecules reinforces that by CO<sub>2</sub> via the water vapor feedback

Workshops #4,5: logarithmic dependence global warming potential

### Conclusions

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- Greenhouse effect of water vapor leads to a positive feedback on CO<sub>2</sub> increase
- The Global warming potential of other GHGs depends on both their efficiency and life time, CO<sub>2</sub> has an especially long life time in the atmosphere
Global Warming Science 101, Greenhouse, Camille Hankel & Eli Tziperman

## The End